

# Octupole deformation in light actinides

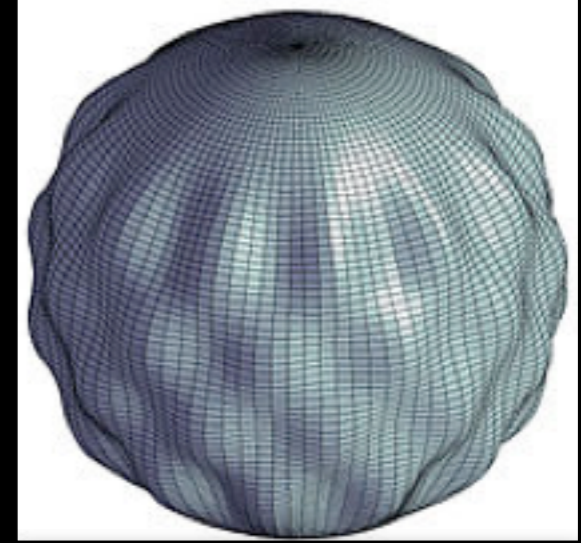
Andriana Martinou

Institute of Nuclear and Particle Physics N.C.S.R.  
“Demokritos”

# Collective model

- ✦ The multipole expansion of the nuclear radius is:

$$R = R_0 \left( 1 + \sum_{\lambda, \mu} \alpha_{\lambda, \mu}^* Y_{\lambda, \mu}(\theta, \phi) \right)$$

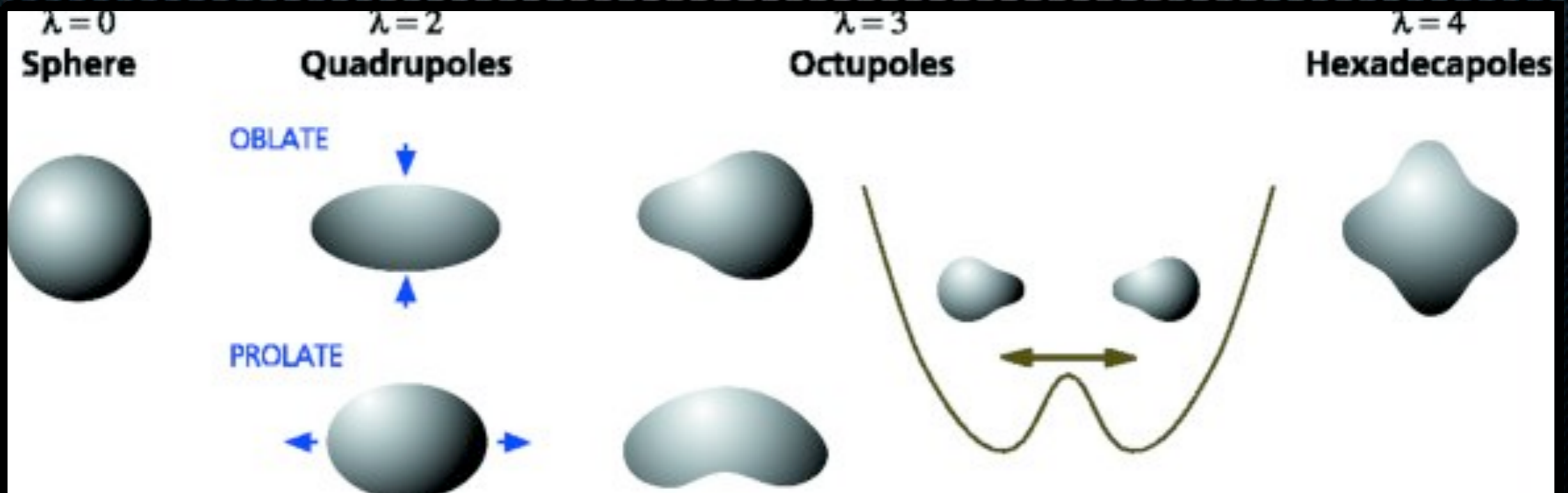


The nuclear surface oscillates.

- ✦  $\lambda=2$   $\longrightarrow$  Quadrupole deformation
- ✦  $\lambda=3$   $\longrightarrow$  Octupole deformation

# Deformation types

- Equal potential multipole shapes:



# AQQA symmetric model

- Both quadrupole and octupole deformations are taken into account, with the deformation axes to coincide.
- The Hamiltonian of the AQQA is:

$$\hat{H} = \sum_{\lambda=2,3} \hat{T}_{\lambda} + \hat{V}_{eff,\lambda}(\beta_2, \beta_3)$$

$\beta_2, \beta_3$

quadrupole and octupole  
deformation variables

$B_2, B_3$

Mass  
parameters

D. Bonatsos, D. Lenis, N. Minkov, D. Petrellis, and P. Yotov,  
Phys. Rev. C 71, 064309 (2005)

# Polar Transformation

$$\beta_2 = \sqrt{\frac{B_2 + B_3}{2B_2}} \beta \cos\phi, \beta_3 = \sqrt{\frac{B_2 + B_3}{2B_3}} \beta \cos\phi, \beta \in [0, +\infty), \phi \in \left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$$

•  $\varphi=0$



pure quadrupole deformation

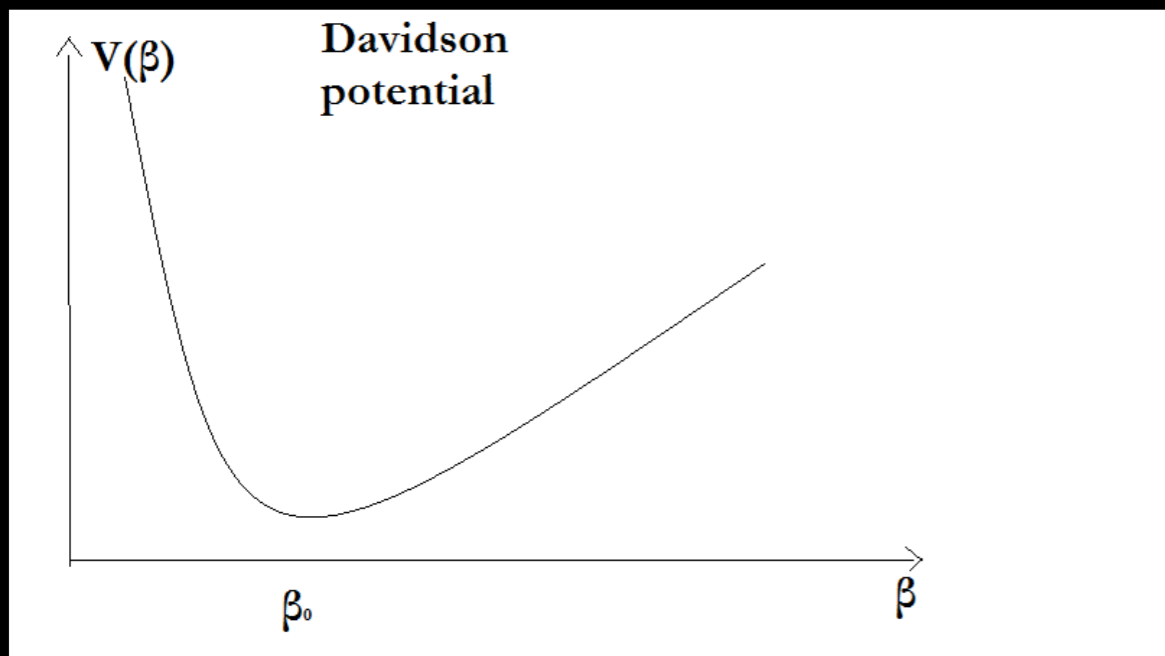
•  $\varphi=\pm\pi/2$



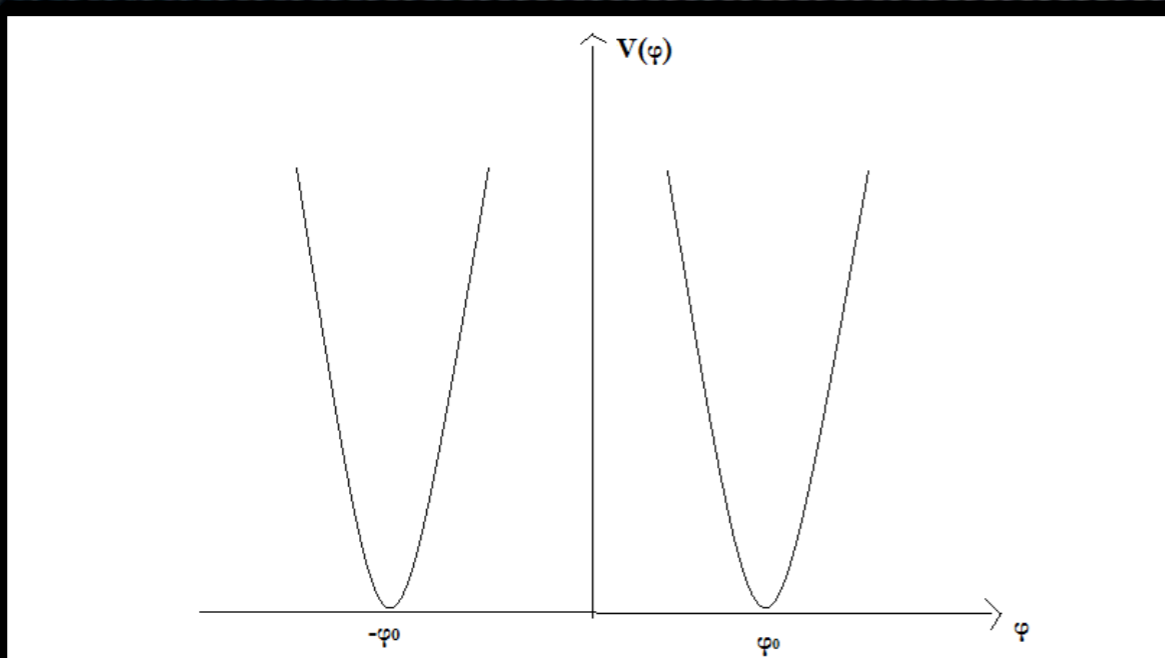
pure octupole deformation

# Potentials

$$V(\beta, \varphi) = V(\beta) + V(\varphi)$$



**exactly solvable  
Davidson  
potential**



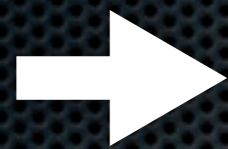
**two harmonic  
oscillators  
centered at  $\pm\varphi_0$**

D. Bonatsos, A. Martinou, N. Minkov, S. Karampagia  
and D. Petrellis, to be published.

# Quadrupole + Octupole = ?

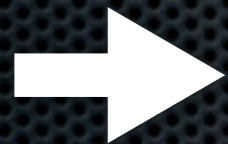


+



When the two oscillations occur with the same frequency and phase, a permanent octupole deformation appears, that it seems to rotate.

**Octupole rotation**



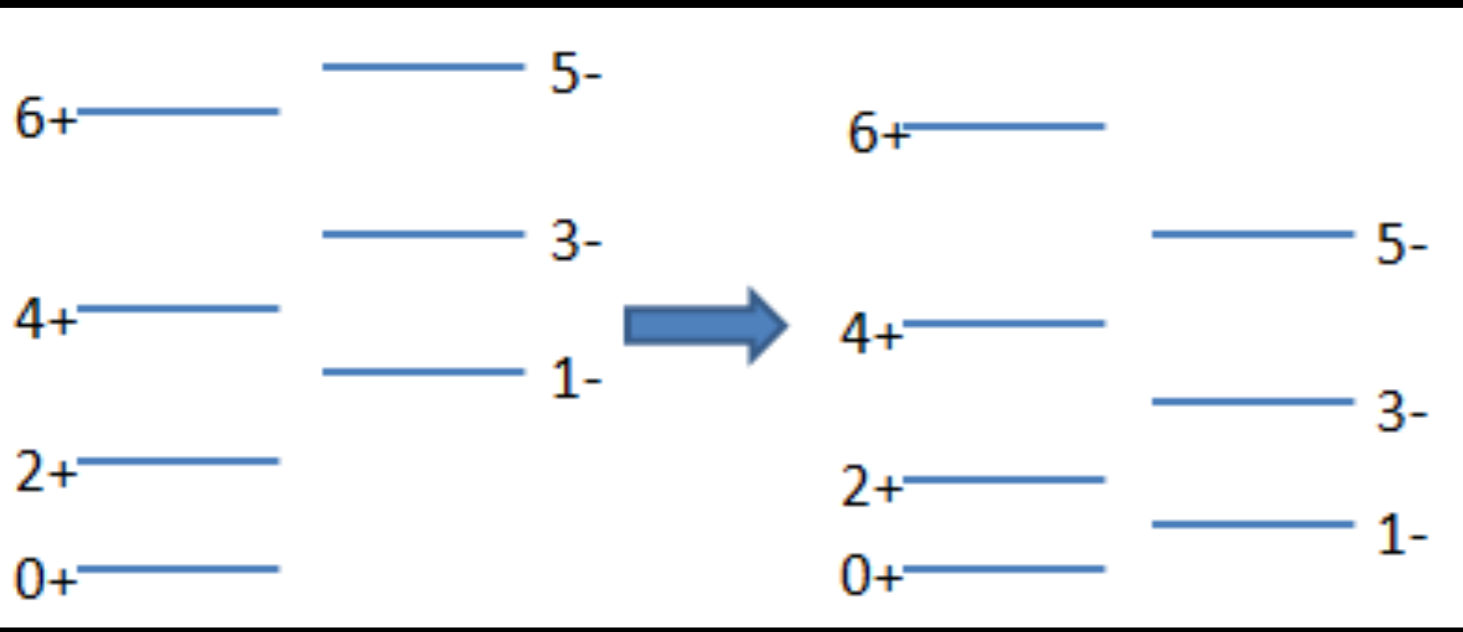
When the two oscillations occur with different frequency and phase, the shape is not constant.

**Octupole vibration**

# Energy levels

Octupole  
vibration

Octupole  
rotation



The displacement of the odd L levels is called **staggering** effect.

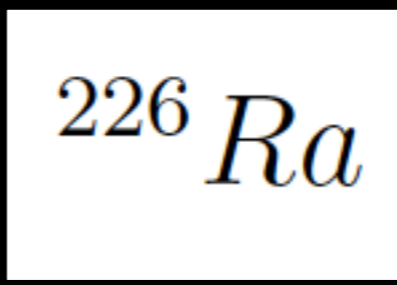
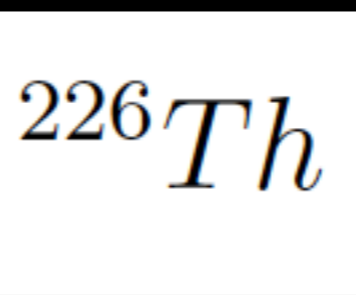
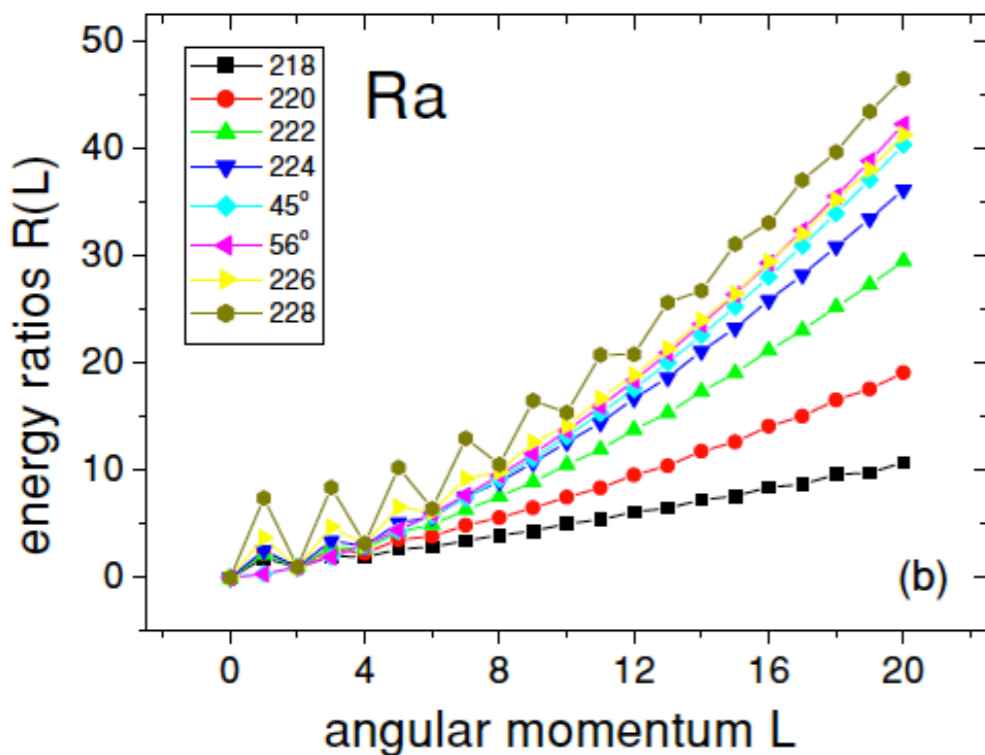
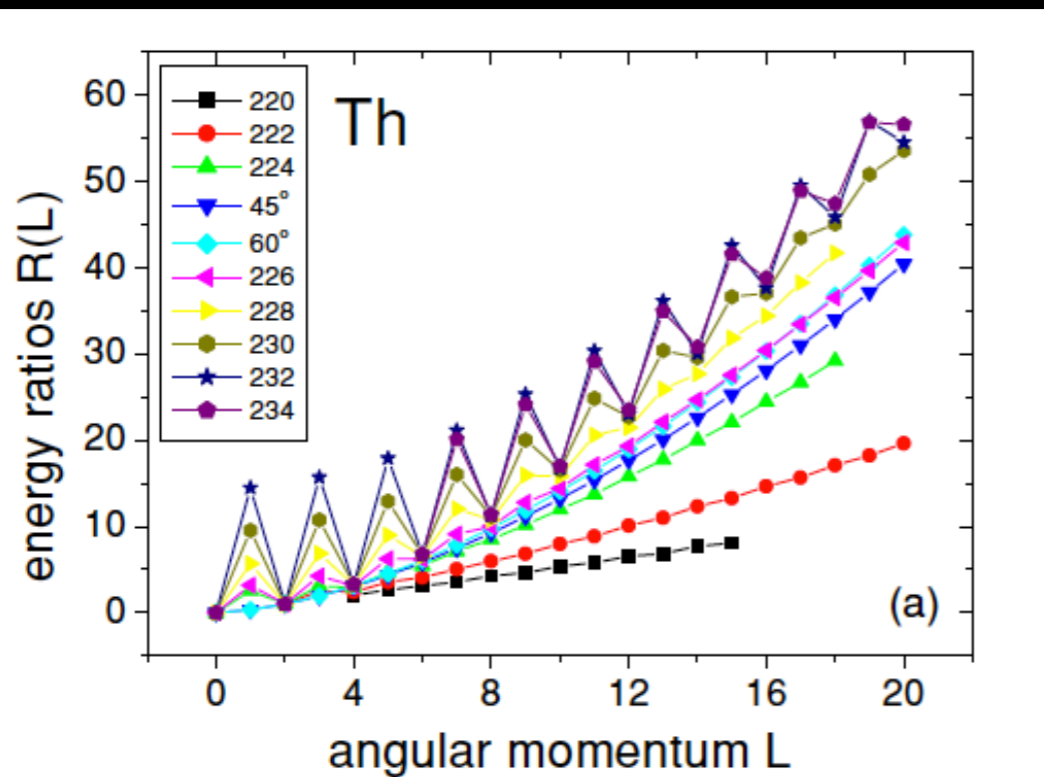
$$\Delta E(L) > 0$$

$$\Delta E(L) = 0$$

$$\Delta E(L) = E(L) - \frac{E(L-1) + E(L+1)}{2}$$



# Critical point in Th and Ra



**Critical nucleus  
between octupole  
vibration and  
octupole rotation**

# Experimental realization

$^{224}\text{Ra}$

Inter-band transitions are supposed to be very small, but instead they proved to be high!

m.e.	exp.	th.
$\langle 0^+    E2    2^+ \rangle$	$199 \pm 3$	196
$\langle 2^+    E2    4^+ \rangle$	$315 \pm 6$	323
$\langle 4^+    E2    6^+ \rangle$	$405 \pm 15$	426
$\langle 6^+    E2    8^+ \rangle$	$500 \pm 60$	525
$\langle 1^-    E2    3^- \rangle$	$230 \pm 11$	236
$\langle 3^-    E2    5^- \rangle$	$410 \pm 60$	334
$\langle 0^+    E2    2^+_{\gamma} \rangle$	$23 \pm 4$	36
$\langle 0^+    E3    3^- \rangle$	$940 \pm 30$	1006
$\langle 2^+    E3    1^- \rangle$	$1370 \pm 140$	1137
$\langle 2^+    E3    3^- \rangle$	$< 4000$	1176
$\langle 2^+    E3    5^- \rangle$	$1410 \pm 190$	1594
$\langle 0^+    E1    1^- \rangle$	$< 0.018$	0.013
$\langle 2^+    E1    1^- \rangle$	$< 0.03$	0.018
$\langle 2^+    E1    3^- \rangle$	$0.026 \pm 0.005$	0.023
$\langle 4^+    E1    5^- \rangle$	$0.030 \pm 0.010$	0.032
$\langle 6^+    E1    7^- \rangle$	$< 0.10$	0.042

L.P. Gaffney, et al., Nature (London) (497), 199 (2013)

# Conclusions

**The AQOA symmetric model provides:**

- ✦ **a) critical point predictions,**
- ✦ **b) energy levels,**
- ✦ **c)  $B(E1)$ ,  $B(E2)$  and  $B(E3)$  calculations.**

**Εὐχαριστώ!**